MATH 1500: Number Concepts for Elementary/Middle School Teachers

Tuesday/Thursday 2 – 3:40 a.m., Spring 2008

Instructor: Dr. Kate Kline
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e-mail: kate.kline@wmich.edu
Office Hours: Mondays 11:00 a.m. to Noon, and by appointment.

Alternative Office Hours offered by other instructors are also available. You will be provided with information on the other instructors’ office hours at the second class meeting.

Overview and Course Description
This course is designed to provide you with opportunities to develop the mathematical understandings crucial to the teaching of number concepts in the elementary grades. As future teachers you need to have a deeper understanding of the mathematical procedures and rules that are central to elementary mathematics in order to more effectively help children learn mathematics with understanding. Thus you will revisit mathematical ideas from the school curriculum with an eye toward understanding those ideas as teachers. You will use innovative elementary and middle school materials to both learn and teach number concepts. Learning and teaching with innovative materials is intended to help you to enrich your conceptions of what mathematical understanding entails, and what it means to learn and teach mathematics for understanding.

Course Format and Participation
This is a laboratory-oriented course in which you will often investigate mathematics collectively (with a partner, in small groups, or whole class). Whole class discussions of different solutions to a problem and the mathematics underlying these solutions will play a central role in this course. Though these discussions will take different forms on different occasions, it will always be the case that your ideas, strategies and questions will guide the discussion. Thus, as a class, we will examine each other’s thinking and come to a better understanding of the mathematics by doing so. Given the student-centered nature of this course, attendance and participation is of the utmost importance. [See attendance policy on the next page.] Satisfactory participation means that you are willing to share your thought process, questions and solutions with the class (even when you don’t think you have “the right answer”), that you support your classmates by listening and thoughtfully reacting to their ideas, and that you attempt all of the homework before class so that you can actively participate in our discussions. Consistent and productive participation in class (see rubric on last page) will be considered in determining final grades in borderline cases assuming the student has a solid passing grade in the class.

Course Prerequisites
• Completion of Math 1100 or a satisfactory score on an appropriate placement exam (ACT, SAT, WMU placement exam). Those not meeting the course prerequisites will be automatically dropped from the course by the Mathematics Department.
• Enrollment is limited to those whose curricula include either Elementary Education or Special Education.

Required Course Materials (available at the bookstore)
• NEW Coursepack for Math 1500 available at the bookstore.

NOTE: If there are no coursepacks at the Bernhard Center bookstore you must:
(1) Fill out an MTO (Made To Order) form at the Information Desk of the bookstore,
(2) PAY for the order at that time, and then (3) pick it up after 10:00 a.m. the next day.
Accommodations
Any student with a documented disability (e.g., physical, learning, psychiatric, vision, hearing, etc.) who needs to arrange reasonable accommodations must contact the professor and the appropriate Disability Services office at the beginning of the semester. If you believe you need some type of accommodation due to a disability and haven’t yet talked with the Disabled Student Resources and Services office, here is their contact information: 2210 Wilbur Ave (across from Rood before the Health Center, above the Day Care Center); 269-387-2116; http://www.dsrs.wmich.edu.

Policy on Incompletes
Three conditions must be met for an incomplete: (1) you must have completed most of the coursework; (2) your current grade is DC or better; and (3) circumstances beyond your control prevent the completion of the coursework on time. All incomplete grades must be approved by the Chair of the Mathematics Department.

Academic Integrity
You are responsible for making yourself aware of and understanding the policies and procedures in the Undergraduate and Graduate Catalogs that pertain to Academic Honesty. These policies include cheating, fabrication, falsification and forgery, multiple submission, plagiarism, complicity and computer misuse. [The policies can be found at www.www.wmich.edu/catalog under Academic Policies, Student Rights and Responsibilities.] If there is reason to believe you have been involved in academic dishonesty, you will be referred to the Office of Student Conduct. You will be given the opportunity to review the charge(s). If you believe you are not responsible, you will have the opportunity for a hearing. You should consult with me if you are uncertain about an issue of academic honesty prior to the submission of an assignment or test.

E-mail Policy
The only email address that I will use to communicate with you is the one associated with a BroncoNet ID. You can access this email account or get instructions for obtaining a BroncoNet ID at GoWMU.wmich.edu. [Typical form of account name: firstname.middlename.lastname@wmich.edu or firstname.middleinitial.lastname@wmich.edu.]

Grading Policy
If all course requirements have been met, grades will be assigned according to the scale:

- 93 – 100%  A
- 88 – 92%  BA
- 82 – 87%  B
- 77 – 81%  CB
- 71 – 76%  C
- Below 60%  E

DC
- 66% - 70%
- 60% - 65%
- D

NOTES: You must attain at least a C (71% or higher) in this course in order to take Math 1510 and Math 2650. If you intend to pursue the Elementary Mathematics Minor, you must attain at least a B (82% or higher) in all elementary mathematics courses.

Course Requirements
The following is a tentative outline of the required graded assignments and their weights:
- Exams  ≈ 37% of final grade
- Comprehensive Final  ≈ 28% of final grade
- Other Assignments  ≈ 35% of final grade
  (e.g. writing assignments, reading reflections, homework, etc.)
Attendance Policy & Related Responsibilities
As much of the course content is presented in a small-group, problem-solving format, daily attendance is required. Not only do excessive absences suggest a lack of professionalism and commitment, but they also guarantee that you will not attain the objectives of this course. Your final grade will be lowered by one letter if you have more than two absences, excused or non-excused. If you have excessive absences (more than 4 for the semester), you will not receive higher than a grade of C regardless of your performance on assignments and exams. Attendance will be taken at the beginning of class. If you are late, it is your responsibility to notify me (after class) of your presence. If you arrive late or leave early more than twice, each tardy or early leave will count as half an absence.

In the event that you must be absent from class, it is your responsibility to:
1) Let me know before the missed section (or soon after) if all possible, either by phone or email;
2) Obtain the notes and homework assignment from a peer;
3) Review those notes and complete the homework;
4) After you have reviewed the notes and worked on homework, make an appointment with me to discuss any questions you have about the materials.

Course Notebook
We recommend that you organize your work for this course in a notebook (e.g. one-inch three-ring binder) that includes the following sections: 1) In-class & Post-class Notes, 2) Homework, and 3) Reading Notes and Reflections. Your aim should be to make your notebook into something that will serve as a resource for you over time. Items within your notebook will be assessed through various means. Therefore, it is critical to always bring your notebook to class with you, and to keep up on your daily work and seek help when you don’t understand an assignment. Here are suggestions for each section of your notebook.

In-class & Post-class Notes: It is often the case that you may have difficulty taking notes on the discussions that occur during class. For this reason we strongly recommend that you take at least 10 minutes after each class to capture important mathematical ideas that have been discussed during class. This will help to solidify your understanding, and highlight areas/issues around which you still have questions.

Homework: In general, we did not provide enough room for you to do the homework on the coursepack pages. Therefore it is recommended that you copy each problem into your notebook before solving the problem.

Reading Notes: Your notes on readings should include a minimum of 3-5 main points from each reading, along with whatever explanation or examples necessary to make these notes useful. For all readings, be sure to indicate the page numbers and book or unit where the readings can be found. On occasion you may be asked to write a reflection on a particular question or on a group of readings. These reflections should also be kept in this section.

Assignments
Assignments must be typed and turned in by the specified due date (and time). Only one late assignment will be accepted per semester as long as it is turned in before the assignment has been discussed in class, or the graded assignments have been returned; the grade of a late assignment will be automatically lowered by one letter grade per day (24 hour period). Homework and reading notes may be handwritten, unless otherwise specified.

Exams
Make-up exams will only be given under extreme and unavoidable circumstances, and must be taken before graded exams are returned to the rest of the class.
<table>
<thead>
<tr>
<th>DATE</th>
<th>Homework Due (may be collected)</th>
<th>Collected Assessments</th>
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<tbody>
<tr>
<td>January 8</td>
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<tr>
<td>10</td>
<td>WN-1: Divisibility Rule for 4 &amp; Renaming Numbers</td>
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<td></td>
<td><strong>Read:</strong> <em>The Limits of Learning Rules</em></td>
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<td>15</td>
<td>WN-2: Subtraction Starters, Part 1</td>
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<td><strong>E-mail by ____________;</strong> 3 story problems for 86 – 29</td>
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<td><strong>Read:</strong> <em>How Many Steps to 10,000?</em></td>
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<td><strong>Read:</strong> <em>CP-74: Integer in Two Ways</em></td>
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<td><strong>CP-75: Integer in Two Ways</strong></td>
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<td>17</td>
<td>WN-3: Subtraction Starters, Part 2</td>
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<td>WN-4: Representations as Starters for Subtraction</td>
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<td><strong>CP-76: Integer in Two Ways</strong></td>
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<td>22</td>
<td>WN-6 Solving Subtraction Problems in Different Ways</td>
<td>Writing # 1</td>
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<td>WN-7 Addition Starter Problems</td>
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<td><strong>Writing #1 (WN-5): Justifying One Strategy in Two Ways</strong></td>
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<td>24</td>
<td>WN-8 Solving Addition Problems in Different Ways</td>
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<td>WN-9 What Strategies Do You Use? (A only)</td>
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<td><strong>Read &amp; Reflect (p.110): Developing Teachers’ Computational Fluency; Reasoning and Proof in Math, Part 1; and Representing Subtraction on the Number Line</strong></td>
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<td>29</td>
<td><strong>Read:</strong> <em>Images of Multiplication; About Cluster Problems</em></td>
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<td>WN-10 Multiplication Starters</td>
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<td>Multiplication Cluster Problems, #3</td>
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<td><strong>CP-77: Integer in Two Ways</strong></td>
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<td>31</td>
<td>WN-12 Multiplication More Than One Way</td>
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<td>Multiplication Starter Problems, #1 &amp; 4</td>
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<td>February 5</td>
<td><strong>WN-15 More Multiplication Clusters</strong></td>
<td>Writing # 2</td>
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<td><strong>Read:</strong> <em>Multiplying by Multiples of Ten; What Does it Mean to “Add a Zero;”</em> and <em>Reasoning and Proof in Mathematics, Part 2</em></td>
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<td><strong>Writing #2 (WN-13):</strong> Fixing Student’s Strategy &amp; Justifying it in Two Ways</td>
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<td>7</td>
<td>WN-16 Generating Interpretations for Starters</td>
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<td><strong>Read:</strong> <em>Two Kinds of Division;</em> and <em>The Relationship Between Multiplication &amp; Division</em></td>
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<td>12</td>
<td>Division Cluster Problems, #2, 4</td>
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<td>14</td>
<td><strong>CP-78: Integer in Two Ways</strong></td>
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<td>19</td>
<td>Division Cluster Problems, #5, 6, &amp; 7</td>
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<td><strong>EXAM 1</strong></td>
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| 21   | Read: CP-79 & 80, *Fraction Balance (Directions)*  
CP- 81: Fraction Balances         |                        |
| 26   | FR-2: Fractions Larger Than One  
FR-3: Representations with Parts & Wholes |                        |
| 28   | FR-5: Extending Classwork from the Bagel Problems  
CP- 82 & 83: Fraction Balances  
Read: *Keeping Track of the Whole; Fraction Meanings* |                        |

**March 3-7**  
*SPRING BREAK*

**March 11**  
FR-7: Fraction Comparison Extensions  
Read: CP- 84 & 85: *Fraction Two Ways (directions)*  
CP- 86: Fraction Two Ways  
Read: *Creating, Naming and Justifying Fractions, pt. 1*

**13**  
FR-9: Reasoning for Fraction Addition & Subtraction  
CP- 87: Fraction Two Ways  
Read: *Activities 7 – 9; and Strategies for Comparing Fractions*

**18**  
FR-10 Fraction Computation  
FR-11 Stories for Fraction Multiplication  
CP- 88: Fraction Two Ways

**20**  
FR-12 Reasoning w/ Fractions in Context  
FR-13 Exploring Stories & Diagrams

**25**  
FR-15 Operating with Fractions  
FR-16 More Operating w/ Fractions  
Read: *What Do You Do with the Remainders? and Creating, Naming and Justifying Fractions, pt. 2*

**27**  
FR-18 More Division Stories  
FR 19 Fraction Consolidation Problems

**April 1**  
**EXAM 2**  
Exam 2

**3**  
Read: CP- 90 – 92: *Decimal Two Ways (Directions)*  
CP- 93, 94: Decimal Two Ways

**8**  
DN-2 Ordering Decimals  
CP- 95, 96: Decimal Two Ways

**10**  
DN-4 Complete Table & Generate Patterns & Conjectures  
DN-5 What Happens When You Change Places?  
CP- 97, 98: Decimal Two Ways

**15 & 17**  
Read: *Extending Place Value to Thousandths and Beyond; Finding Decimal Equivalents of Fractions by Division; and Connecting Fractions & Decimals*

**April 21**  
Monday, December 21st 2:45 p.m. – 4:45 p.m.  
Final Exam
### Class Participation Rubric

Class participation will be informally assessed on a continuing basis. Class participation grades will be based on participation in both small group and whole group settings.

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<th>Grade</th>
<th>Description</th>
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| **A** | Contributing to Others’ Learning  
This is the goal of the class. This does NOT mean telling or showing someone else how to do something. Sometimes it means sharing your thinking about the mathematics so that others can analyze and learn from it. Always it means listening carefully to what others are saying, connecting what you hear to your own thinking, and asking questions that will help everyone involved better understand the mathematics. The expectations for receiving this grade will increase as the semester goes on. That is, it is assumed that these are skills that you are learning so in the beginning attempts at doing this will be sufficient to earn the grade. As you learn more about student thinking and develop these skills, it will require competence in them to earn the A. |
| **B** | Contributing to One's Own Learning  
Here you are clearly engaged in learning the mathematics, but haven’t moved outside yourself to interact well with others. It generally means doing quality work, but not being willing to share your thinking with others or not showing interest in making sense of their thinking. In the context of whole class discussion, it would mean listening and learning, but not sharing your ideas or observations with the class. |
| **C** | Getting By  
This involves showing up, minding your own business, and doing what you are told. |
| **D** | Interfering with Learning of Self or Others  
There are various ways one can do this; the most obvious are distracting group members from the task at hand or being belligerent about what one is asked to do. More subtle ways include implying someone is stupid because they don’t understand a problem or telling someone how to do a problem and thus undercutting their opportunity to figure it out for themselves. |
| **F** | Not there  
This includes not being there physically and/or mentally. Note that whenever you are absent, it is your responsibility to make up the work, preferably before the next class so that you are able to participate in class. See syllabus for responsibilities associated with missing class. |