

### X3.6d

205

PHYS-205(6) (Kaldon-40534)  
 WMU-Fall 2000

Name \_\_\_\_\_

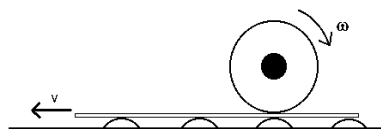
Exam 3 - 100,000 points + 20,000 ☆ points

11/16/2000•Rev.6

**State Any Assumptions You Need To Make – Show All Work – Circle Any Final Answers**  
**Use Your Time Wisely – Work on What You Can – Be Sure to Write Down Equations**  
**Feel Free to Ask Any Questions**     ☆2a    ☆2b    ☆2c    ☆2e

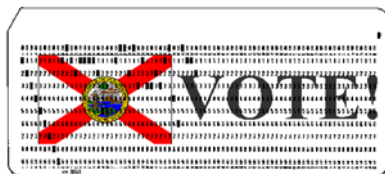
**“And Now We Take You To Palm Beach County, Florida...” (50,000 points)**

1.) (a) Suppose you suddenly have 400,000 computer punch card ballots to run through a counting machine. Each card ( $m = 0.000454 \text{ kg}$ ) has to move 20.0 cm (0.200 m) in 1.00 seconds. A spinning drive wheel of 6.00 cm diameter (0.0600 m) moves the cards along. Find the angular velocity,  $\omega$ , of the drive wheel.

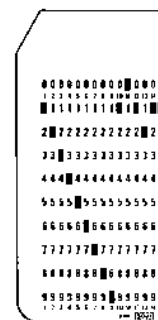
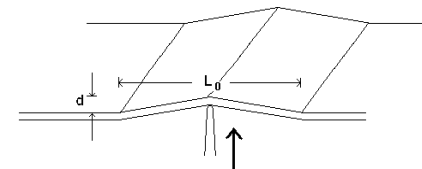


(b) The solid drive wheel has a mass of 50.0 grams (0.0500 kg). Find the rotational kinetic energy of the drive wheel. *If you did not get an answer to (a), use  $\omega = 20.0 \text{ rad/sec}$ .*

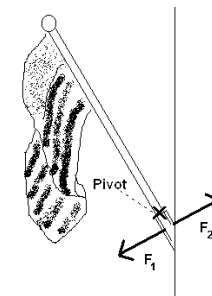
(c) Suddenly a card jams in the machine and the system automatically stops. Find the angular acceleration  $\alpha$  to bring the drive wheel to a stop in a single rotation. *If you did not get an answer to (a), use  $\omega_0 = 20.0 \text{ rad/sec}$ .*



(d) One of the problems with the ballots in parts of Florida is *chads* – the small bits of the cards that are supposed to be punched out. If you just push on a region of the card, you may stretch the material as shown in the illustration – let us assume that this is a tension force problem, with  $T = 10.0 \text{ N}$ . Consider a card that is  $0.100 \text{ mm} = 0.000100 \text{ m}$  thick, where the size of the stretched region is  $L_0 = 2.00 \text{ mm} = 0.00200 \text{ m}$  and  $2.00 L_0$  deep. The material is depressed by  $d = 0.250 \text{ mm} = 0.000250 \text{ m}$ . Find the Young's Modulus,  $Y_m$ , of the card material.



(e) A U.S. flag hangs from a bracket wall. The flag and pole provide a positive torque,  $\tau = 30.0 \text{ N}\cdot\text{m}$ , about a pivot point at the end of the bracket. To keep the flag from falling, a force perpendicular to the flagpole is applied 7.00 cm from the pivot point. Determine if this force is  $F_1$  or  $F_2$ , and then find the magnitude of this force.



**So You Think You've Got Star Problems? When I Was A Kid... (50,000 points)**

2.) ☆(a) A plate of mass  $m = 6.00$  kg has dimensions  $a = 1.50$  m and  $b = 0.720$  m.

Find the center of mass coordinate  $x_{cm}$  by integrating  $x_{cm} = \frac{1}{M} \int x dm$ .



☆(b) A plate of mass  $m = 6.00$  kg has dimensions  $a = 1.50$  m and  $b = 0.720$  m. Find the moment of inertia  $I$  of the plate about an axis along the left edge as shown, by integrating  $I = \int r^2 dm$ .



☆(c) A simple harmonic oscillator has an acceleration given as  $a(t) = 1.00m/s^2 (\cos(\omega t))$ . Find  $x(t)$ .

(d) Bob weighs 981 N on the surface of the Earth. What would his weight be on the planet Mercury?  
 $M_M = 3.18 \times 10^{23}$  kg,  $R_M = 2.43 \times 10^6$  m,  $g = 9.81$  m/s<sup>2</sup>,  $G = 6.67 \times 10^{-11}$  N·m<sup>2</sup>/kg<sup>2</sup>.

☆(e) A torque  $\vec{\tau}$  to tighten a bolt consists of a force being applied at a distance from the axis of rotation. As the bolt gets tighter, it gets harder and harder to turn the bolt, so the torque as a function of angle is given by  $\tau = \sqrt{C\theta}$ , where C is some constant with appropriate units. If the total work done by applying this torque through two complete revolutions is 1500. J, then find C.

