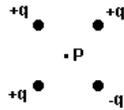


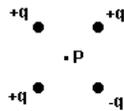
State Any Assumptions You Need To Make – Show All Work – Circle Any Final Answers
Use Your Time Wisely – Work on What You Can – Be Sure to Write Down Equations
Feel Free to Ask Any Questions ☆2a ☆2b ☆2c ☆2e

“Dr. Phil, Dr. Phil—I’m Still Seeing Spots In Front Of My Eyes!” (50,000 pts.)

1.) Four charges, $|q| = 7.00 \times 10^{-6} \text{ C}$, are rigidly arranged in a square ($L = 10.0 \text{ cm} = 0.100 \text{ m}$) as shown.
 (a) Using symmetry, draw a simpler system that would have the same electric field vector at P, but fewer charges (less things to calculate).

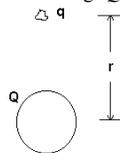


(b) Find the electric field vector, \vec{E}_{total} , at the center of the square of charges at point P.



(c) A small bit of dust, mass $= 1.38 \times 10^{-6} \text{ kg}$, has 13,800,000 extra electrons on it. Find the charge q .

(d) Our little piece of dust with charge q is $r = 1.54 \text{ cm}$ above a spherical metal conductor with charge Q as shown. Find the value of Q such that the piece of dust does not fall (or rise).

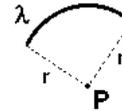


(e) If the potential V is zero, must the electric field, E , be zero as well? *Short answer.*

Another Stupid Star Problem (50,000 points)

2.) ☆(a) A cylindrical insulator of radius R and length L has a total charge Q evenly distributed throughout the cylinder. Use Gauss’ Law to find the magnitude of the E-field at a radius r , where $r < R$.
 NOTE: You may evaluate the integrals by using the known equations for things like the surface area and volume of a cylinder.

☆(b) Use direct integration to find the magnitude of the potential V for a quarter-circle line of charge of radius $r = 1.00 \text{ m}$ and $\lambda = 1.00 \times 10^{-4} \text{ C/m}$, at a point P at the center of the circle. $V=0$ at infinity.



☆(c) An electric potential is given by $V_a = (1.38 \text{ V}) + (1.38 \text{ V/m})x + (1.38 \text{ V/m}^2)x^2 + (1.38 \text{ V/m}^3)y^3$. Find E_x .

(d) A charge Q sits on a small conducting sphere. Nearby is a wedge shaped Gaussian surface designed so that the E -field from Q only goes through the left and right sides at radius $r = a$ and $r = b$, respectively. What is the total electric flux, Φ_E , through the Gaussian surface?



☆(e) An electron is 5.00 cm from a sheet of charge ($\sigma = 1.38 \times 10^{-5} \text{ C/m}^2$). Find the work due to the electric force to move the electron to only 2.50 cm from the sheet of charge, by integrating $\int_a^b F_E(x) dx$.