

INVERSE TRIGONOMETRIC FORMS

$$87. \int \sin^{-1} u \, du = u \sin^{-1} u + \sqrt{1-u^2} + C$$

$$88. \int \cos^{-1} u \, du = u \cos^{-1} u - \sqrt{1-u^2} + C$$

$$89. \int \tan^{-1} u \, du = u \tan^{-1} u - \frac{1}{2} \ln(1+u^2) + C$$

$$90. \int u \sin^{-1} u \, du = \frac{2u^2-1}{4} \sin^{-1} u + \frac{u\sqrt{1-u^2}}{4} + C$$

$$91. \int u \cos^{-1} u \, du = \frac{2u^2-1}{4} \cos^{-1} u - \frac{u\sqrt{1-u^2}}{4} + C$$

$$92. \int u \tan^{-1} u \, du = \frac{u^2+1}{2} \tan^{-1} u - \frac{u}{2} + C$$

$$93. \int u^n \sin^{-1} u \, du = \frac{1}{n+1} \left[u^{n+1} \sin^{-1} u - \int \frac{u^{n+1} du}{\sqrt{1-u^2}} \right], n \neq -1$$

$$94. \int u^n \cos^{-1} u \, du = \frac{1}{n+1} \left[u^{n+1} \cos^{-1} u + \int \frac{u^{n+1} du}{\sqrt{1-u^2}} \right], n \neq -1$$

$$95. \int u^n \tan^{-1} u \, du = \frac{1}{n+1} \left[u^{n+1} \tan^{-1} u - \int \frac{u^{n+1} du}{1+u^2} \right], n \neq -1$$

EXPONENTIAL AND LOGARITHMIC FORMS

$$96. \int u e^{au} \, du = \frac{1}{a^2} (au-1)e^{au} + C$$

$$97. \int u^n e^{au} \, du = \frac{1}{a} u^n e^{au} - \frac{n}{a} \int u^{n-1} e^{au} \, du$$

$$98. \int e^{au} \sin bu \, du = \frac{e^{au}}{a^2+b^2} (a \sin bu - b \cos bu) + C$$

$$99. \int e^{au} \cos bu \, du = \frac{e^{au}}{a^2+b^2} (a \cos bu + b \sin bu) + C$$

$$100. \int \ln u \, du = u \ln u - u + C$$

$$101. \int u^n \ln u \, du = \frac{u^{n+1}}{(n+1)^2} [(n+1) \ln u - 1] + C$$

$$102. \int \frac{1}{u \ln u} \, du = \ln |\ln |u|| + C$$

HYPERBOLIC FORMS

$$103. \int \sinh u \, du = \cosh u + C$$

$$104. \int \cosh u \, du = \sinh u + C$$

$$105. \int \tanh u \, du = \ln \cosh u + C$$

$$106. \int \coth u \, du = \ln |\sinh u| + C$$

$$107. \int \operatorname{sech} u \, du = \tan^{-1} |\sinh u| + C$$

$$108. \int \operatorname{csch} u \, du = \ln \left| \tanh \frac{1}{2} u \right| + C$$

$$109. \int \operatorname{sech}^2 u \, du = \tanh u + C$$

$$110. \int \operatorname{csch}^2 u \, du = -\coth u + C$$

$$111. \int \operatorname{sech} u \tanh u \, du = -\operatorname{sech} u + C$$

$$112. \int \operatorname{csch} u \coth u \, du = -\operatorname{csch} u + C$$

FORMS INVOLVING $\sqrt{2au-u^2}$

$$113. \int \sqrt{2au-u^2} \, du = \frac{u-a}{2} \sqrt{2au-u^2} + \frac{a^2}{2} \cos^{-1} \left(\frac{a-u}{a} \right) + C$$

$$114. \int u \sqrt{2au-u^2} \, du = \frac{2u^2-au-3a^2}{6} \sqrt{2au-u^2} + \frac{a^3}{2} \cos^{-1} \left(\frac{a-u}{a} \right) + C$$

$$115. \int \frac{\sqrt{2au-u^2}}{u} \, du = \sqrt{2au-u^2} + a \cos^{-1} \left(\frac{a-u}{a} \right) + C$$

$$116. \int \frac{\sqrt{2au-u^2}}{u^2} \, du = -\frac{2\sqrt{2au-u^2}}{u} - \cos^{-1} \left(\frac{a-u}{a} \right) + C$$

$$117. \int \frac{du}{\sqrt{2au-u^2}} = \cos^{-1} \left(\frac{a-u}{a} \right) + C$$

$$118. \int \frac{u \, du}{\sqrt{2au-u^2}} = -\sqrt{2au-u^2} + a \cos^{-1} \left(\frac{a-u}{a} \right) + C$$

$$119. \int \frac{u^2 \, du}{\sqrt{2au-u^2}} = -\frac{(u+3a)}{2} \sqrt{2au-u^2} + \frac{3a^2}{2} \cos^{-1} \left(\frac{a-u}{a} \right) + C$$

$$120. \int \frac{du}{u \sqrt{2au-u^2}} = -\frac{\sqrt{2au-u^2}}{au} + C$$